

UNIVERSIDAD NACIONAL DE ENTRE RIOS
FACULTAD DE INGENIERIA
CENTRO DE MEDIOS
BIBLIOTECA

W1409

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^{*}An asterisk indicates an advanced topic area that may be omitted from the course of study with no loss in continuity to later material.

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