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Preface to the Dover Edition

Preface to the First Edition

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## ***Preface to the Dover Edition***

The gratifying reception accorded to this work has encouraged me to continue to search for improvements, all of which have been inserted into this Dover edition. I take this opportunity to express my thanks to the hundreds of academicians and students who contacted me regarding this text. I am also grateful to Alan Weissman and John Grafton of Dover Publications for their careful attention to typographical detail, so important in a work of this kind.

*R. A. Granger*

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