

# **Introduction to Autonomous Mobile Robots**

second edition

Roland Siegwart, Illah R. Nourbakhsh, and Davide Scaramuzza

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**Contents****Acknowledgments**

xiii

xiv

**Preface**

xv

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Introduction	1
1.2	An Overview of the Book	11
<b>2</b>	<b>Locomotion</b>	<b>13</b>
2.1	Introduction	13
2.1.1	Key issues for locomotion	16
2.2	Legged Mobile Robots	17
2.2.1	Leg configurations and stability	18
2.2.2	Consideration of dynamics	21
2.2.3	Examples of legged robot locomotion	25
2.3	Wheeled Mobile Robots	35
2.3.1	Wheeled locomotion: The design space	35
2.3.2	Wheeled locomotion: Case studies	43
2.4	Aerial Mobile Robots	50
2.4.1	Introduction	50
2.4.2	Aircraft configurations	52
2.4.3	State of the art in autonomous VTOL	52
2.5	Problems	56
<b>3</b>	<b>Mobile Robot Kinematics</b>	<b>57</b>
3.1	Introduction	57
3.2	Kinematic Models and Constraints	58

3.2.1	Representing robot position	58
3.2.2	Forward kinematic models	61
3.2.3	Wheel kinematic constraints	63
3.2.4	Robot kinematic constraints	71
3.2.5	Examples: Robot kinematic models and constraints	73
3.3	Mobile Robot Maneuverability	77
3.3.1	Degree of mobility	77
3.3.2	Degree of steerability	81
3.3.3	Robot maneuverability	82
3.4	Mobile Robot Workspace	84
3.4.1	Degrees of freedom	84
3.4.2	Holonomic robots	85
3.4.3	Path and trajectory considerations	87
3.5	Beyond Basic Kinematics	90
3.6	Motion Control (Kinematic Control)	91
3.6.1	Open loop control (trajectory-following)	91
3.6.2	Feedback control	92
3.7	Problems	99
<b>4</b>	<b>Perception</b>	<b>101</b>
4.1	Sensors for Mobile Robots	101
4.1.1	Sensor classification	101
4.1.2	Characterizing sensor performance	103
4.1.3	Representing uncertainty	109
4.1.4	Wheel/motor sensors	115
4.1.5	Heading sensors	116
4.1.6	Accelerometers	119
4.1.7	Inertial measurement unit (IMU)	121
4.1.8	Ground beacons	122
4.1.9	Active ranging	125
4.1.10	Motion/speed sensors	140
4.1.11	Vision sensors	142
4.2	Fundamentals of Computer Vision	142
4.2.1	Introduction	142
4.2.2	The digital camera	142
4.2.3	Image formation	148
4.2.4	Omnidirectional cameras	159
4.2.5	Structure from stereopsis	169
4.2.6	Structure from motion	180

4.2.7	Motion and optical flow	188
4.2.8	Color tracking	191
4.3	Fundamentals of Image Processing	194
4.3.1	Image filtering	195
4.3.2	Edge detection	198
4.3.3	Computing image similarity	205
4.4	Feature Extraction	207
4.5	Image Feature Extraction: Interest Point Detectors	210
4.5.1	Introduction	211
4.5.2	Properties of the ideal feature detector	211
4.5.3	Corner detectors	214
4.5.4	Invariance to photometric and geometric changes	217
4.5.5	Blob detectors	226
4.6	Place Recognition	233
4.6.1	Introduction	233
4.6.2	From bag of features to visual words	233
4.6.3	Efficient location recognition by using an inverted file	234
4.6.4	Geometric verification for robust location recognition	235
4.6.5	Applications	236
4.6.6	Other image representations for place recognition	237
4.7	Feature Extraction Based on Range Data (Laser, Ultrasonic)	240
4.7.1	Line fitting	241
4.7.2	Six line-extraction algorithms	247
4.7.3	Range histogram features	258
4.7.4	Extracting other geometric features	259
4.8	Problems	261
<b>5</b>	<b>Mobile Robot Localization</b>	<b>263</b>
5.1	Introduction	263
5.2	The Challenge of Localization: Noise and Aliasing	264
5.2.1	Sensor noise	265
5.2.2	Sensor aliasing	266
5.2.3	Effector noise	267
5.2.4	An error model for odometric position estimation	268
5.3	To Localize or Not to Localize: Localization-Based Navigation Versus Programmed Solutions	273
5.4	Belief Representation	276
5.4.1	Single-hypothesis belief	276
5.4.2	Multiple-hypothesis belief	278

5.5	Map Representation	282
5.5.1	Continuous representations	282
5.5.2	Decomposition strategies	285
5.5.3	State of the art: Current challenges in map representation	292
5.6	Probabilistic Map-Based Localization	294
5.6.1	Introduction	294
5.6.2	The robot localization problem	295
5.6.3	Basic concepts of probability theory	297
5.6.4	Terminology	300
5.6.5	The ingredients of probabilistic map-based localization	302
5.6.6	Classification of localization problems	304
5.6.7	Markov localization	305
5.6.8	Kalman filter localization	320
5.7	Other Examples of Localization Systems	340
5.7.1	Landmark-based navigation	341
5.7.2	Globally unique localization	342
5.7.3	Positioning beacon systems	344
5.7.4	Route-based localization	345
5.8	Autonomous Map Building	346
5.8.1	Introduction	346
5.8.2	SLAM: The simultaneous localization and mapping problem	347
5.8.3	Mathematical definition of SLAM	349
5.8.4	Extended Kalman Filter (EKF) SLAM	351
5.8.5	Visual SLAM with a single camera	353
5.8.6	Discussion on EKF SLAM	357
5.8.7	Graph-based SLAM	359
5.8.8	Particle filter SLAM	360
5.8.9	Open challenges in SLAM	362
5.8.10	Open source SLAM software and other resources	363
5.9	Problems	363
<b>6</b>	<b>Planning and Navigation</b>	<b>365</b>
6.1	Introduction	365
6.2	Competences for Navigation: Planning and Reacting	366
6.3	Path Planning	367
6.3.1	Graph search	369
6.3.2	Potential field path planning	382
6.4	Obstacle avoidance	389
6.4.1	Bug algorithm	389

## Contents

xi

6.4.2	Vector field histogram	393
6.4.3	The bubble band technique	395
6.4.4	Curvature velocity techniques	397
6.4.5	Dynamic window approaches	398
6.4.6	The Schlegel approach to obstacle avoidance	400
6.4.7	Nearness diagram	401
6.4.8	Gradient method	402
6.4.9	Adding dynamic constraints	402
6.4.10	Other approaches	402
6.4.11	Overview	402
6.5	Navigation Architectures	405
6.5.1	Modularity for code reuse and sharing	406
6.5.2	Control localization	406
6.5.3	Techniques for decomposition	407
6.5.4	Case studies: tiered robot architectures	412
6.6	Problems	419

## Bibliography

421

Books

421

Papers

423

Referenced Webpages

440

## Index

441